# The Crystal Structure of Lithium Hydroxylammonium Sulphate 

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#### Abstract

Crystals of lithium hydroxylammonium sulphate, $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$, are orthorhombic, space group $P b c a$, with $a=18.461$ (5), $b=7.267$ (3), $c=6.695$ (2) $\AA$, $Z=8$. Crystals were grown from an aqueous solution of $\left(\mathrm{NH}_{3} \mathrm{OH}\right)_{2} \mathrm{SO}_{4}$ and $\mathrm{Li}_{2} \mathrm{SO}_{4}$. The structure, which was refined to $R=0.034$ from 1574 X-ray reflexions, contains sheets of $\mathrm{LiSO}_{4}$ hydrogen-bonded together by the $\mathrm{NH}_{3} \mathrm{OH}$ ions. The Li atom is surrounded by four O atoms at $1.96 \AA$ and S by four O at $1.477 \AA$.

Introduction. Single crystals of $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$ were grown by slow evaporation from an aqueous solution * On leave from Laboratoire de Chimie Minérale, E.R.A. 314, Chimie des Matériaux, Faculté des Sciences, Place Eugène Bataillon, 34060 Montpellier, France.


of $\left(\mathrm{NH}_{3} \mathrm{OH}\right)_{2} \mathrm{SO}_{4}$ and $\mathrm{Li}_{2} \mathrm{SO}_{4}$ in stoichiometric quantities. Very thin hexagonal crystals were formed, but recrystallization improved the thickness to a size suitable for X-ray work. The space group was deduced from systematic absences on Weissenberg photographs ard the lattice parameters were measured both for a powder sample and a single crystal; the results, with other crystal data, are given in Table 1. For determination of the structure, a single crystal measuring $0.1 \times 0.1 \times 0.4 \mathrm{~mm}$ was selected. The intensities were measured at room temperature on a Syntex four-circle automatic X-ray diffractometer with Mo $K \alpha$ radiation ( $\lambda=0.71069 \AA$ ) monochromated by reflexion from a graphite crystal. Intensities of 1574 independent reflexions with $\sin \theta / \lambda<0.705$ were measured and cor-

Table 1. Crystallographic data for $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$

| Crystal systemSpace group |  |  |  | Single crystal Orthorhombic |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Pbca |
| $a$ | 18.460 (8) $\AA$ |  |  | 18.461 (5) $\AA$ |
| $b$ | $7 \cdot 280$ (5) |  |  | 7.267 (3) |
| c | $6 \cdot 712$ (3) |  |  | $6 \cdot 695$ (2) |
| $Z$ |  | 8 |  |  |
| $d_{m}$ |  | 2.06 | 10) $\mathrm{g} \mathrm{cm}^{-3}$ |  |
| $d_{x}$ |  | 2.02 | (3) $\mathrm{g} \mathrm{cm}^{-3}$ |  |
| Absorption coefficient | $\begin{aligned} & 5 \cdot 9(\mathrm{Cu} K \alpha) \mathrm{mm}^{-1} \\ & 1.5406 \AA \end{aligned}$ |  |  | $0 \cdot 63\left(\mathrm{Mo} K \alpha\right.$ ) $\mathrm{mm}^{-1}$ |
| Wavelength $K \alpha$ |  |  |  | $0.71069 \AA$ |
| Systematic absences |  | 0kl | $k=2 n+1$ |  |
|  |  | hol | $l=2 n+1$ |  |
|  |  | $h k 0$ | $h=2 n+1$ |  |

Table 2. Parameters derived from the final least-squares refinement
Estimated standard deviations are in parentheses
The expressions used for the temperature factors are:

|  |  |  |  | $\left[-2 \pi^{2} U\right.$ | $\left.\left(\frac{2 \sin \theta}{\lambda}\right)^{2}\right]$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $x$ | $y$ | $z$ | $U$ or $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{12}$ | $U_{13}$ | $U_{23}$ |
| Li | $0 \cdot 2612$ (2) | 0.2535 (8) | $0 \cdot 4122$ (8) | 0.024 (2) | 0.021 (2) | 0.020 (2) | -0.002 (3) | $0 \cdot 000$ (2) | 0.004 (2) |
| S | 0.1559 (1) | 0.0520 (1) | $0 \cdot 1577$ (1) | 0.0127 (2) | 0.0128 (2) | 0.0138 (2) | -0.0000 (3) | 0.0003 (3) | 0.0005 (3) |
| $\mathrm{O}(1)$ | $0 \cdot 3348$ (1) | 0.4390 (3) | 0.3394 (3) | $0 \cdot 022$ (1) | 0.025 (1) | 0.021 (1) | -0.004 (1) | -0.002 (1) | 0.011 (1) |
| $\mathrm{O}(2)$ | $0 \cdot 3289$ (1) | 0.0586 (3) | $0 \cdot 4777$ (3) | 0.025 (1) | 0.024 (1) | 0.018 (1) | $0 \cdot 005$ (1) | 0.001 (1) | 0.007 (1) |
| $\mathrm{O}(3)$ | $0 \cdot 2076$ (1) | 0.2075 (2) | $0 \cdot 1649$ (3) | 0.024 (1) | 0.020 (1) | 0.020 (1) | -0.009 (1) | -0.002 (1) | $0 \cdot 002$ (1) |
| $\mathrm{O}(4)$ | 0.0810 (1) | $0 \cdot 1213$ (3) | $0 \cdot 1458$ (4) | 0.015 (1) | 0.021 (1) | 0.029 (1) | 0.005 (1) | 0.002 (1) | 0.002 (1) |
| $\mathrm{O}(5)$ | $0 \cdot 4468$ (1) | $0 \cdot 1444$ (3) | 0.0716 (3) | 0.034 (1) | 0.034 (1) | 0.036 (1) | -0.001 (1) | 0.001 (1) | 0.009 (1) |
| N | 0.4446 (1) | 0.0037 (4) | 0.2142 (4) | 0.031 (1) | 0.028 (1) | 0.028 (1) | -0.003 (1) | $0 \cdot 006$ (1) | $-0.000(1)$ |
| H(1) | 0.404 (2) | 0.017 (5) | 0.326 (6) | 0.011 (9) |  |  |  |  |  |
| H (2) | 0.429 (2) | -0.109 (5) | $0 \cdot 146$ (5) | 0.012 (9) |  |  |  |  |  |
| H(3) | 0.493 (2) | 0.005 (7) | 0.263 (7) | 0.025 (11) |  |  |  |  |  |
| H(4) | $0 \cdot 400$ (3) | 0.085 (9) | 0.001 (10) | 0.087 (20) |  |  |  |  |  |

rected for Lorentz and polarization effects but not for absorption, which was negligible ( $\mu=0.63 \mathrm{~mm}^{-1}$ ).

The structure was solved from a Patterson synthesis and the hydrogen atoms found from a difference map. The atomic parameters and temperature factors were refined by the full-matrix least-squares program CRYLSQ of the XRAY 71 program library. With anisotropic temperature factors for all non-hydrogen atoms $R_{1}\left[=\sum\left(\left|F_{o}\right|-\left|F_{c}\right|\right) / \sum\left|F_{o}\right|\right]$ was 0.034 . The final $R_{2}\left[=\left(\sum \omega\left(| | F_{o}\left|-\left|F_{c}\right|\right|^{2} / \sum \omega\left|F_{o}\right|^{2}\right)^{1 / 2}\right]\right.$ was $0 \cdot 027$, where $\omega=\left(0 \cdot 1146-0.0044\left|F_{o}\right|+0.00004\left|F_{o}\right|^{2}\right)^{-1}$. Final atomic


Fig. 1. Structure of $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$ projected down a.


Fig. 2. Structure of $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$ projected down $\mathbf{c}$.
positions and temperature factors are given in Table 2.*

Description of the structure. The bond lengths and bond angles are given in Table 3.

Crystals of $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$ are composed of sheets of $\mathrm{LiSO}_{4}$ which are held together by hydrogen bonds from the hydroxylammonium ions. This structure is quite different from the stuffed tetrahedral framework structures of the isoelectronic $\mathrm{Li}\left(\mathrm{N}_{2} \mathrm{H}_{5}\right) \mathrm{SO}_{4}$ (Brown, 1964) and $\mathrm{Li}\left(\mathrm{N}_{2} \mathrm{H}_{5}\right) \mathrm{BeF}_{4}$ (Anderson, Brown \& Vilminot, 1973) or the other compounds of the form $\mathrm{LiMSO}_{4}$ and $\mathrm{LiMBeF}_{4}\left(\mathrm{M}=\mathrm{K}, \mathrm{Rb}, \mathrm{Cs}, \mathrm{NH}_{4}\right)$ discussed by Chung \& Hahn (1972).

## Table 3. Bond distances and angles

$\mathrm{SO}_{4}$ tetrahedron

| S-O(1) | 1.478 (2) $\AA$ |
| :---: | :---: |
| S-O(2) | 1.476 (2) |
| $\mathrm{S}-\mathrm{O}(3)$ | 1.480 (2) |
| S-O(4) | 1.473 (2) |
| $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(2)$ | $110 \cdot 3(1)^{\circ}$ |
| $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(3)$ | 108.8 (1) |
| $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(4)$ | $110 \cdot 1$ (1) |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(3)$ | 108.6 (1) |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(4)$ | 108.7 (1) |
| $\mathrm{O}(3)-\mathrm{S}-\mathrm{O}(4)$ | $110 \cdot 2$ (1) |
| $\mathrm{LiO}_{4}$ tetrahedron |  |
| Li-O(1) | 1.975 (5) $\AA$ |
| $\mathrm{Li}-\mathrm{O}(2)$ | 1.939 (6) |
| Li-O(3) | 1.957 (5) |
| $\mathrm{Li}-\mathrm{O}\left(3^{\prime}\right)$ | $1 \cdot 981$ (5) |
| $\mathrm{O}(1)-\mathrm{Li}-\mathrm{O}(2)$ | 96.4 (2) ${ }^{\circ}$ |
| $\mathrm{O}(1)-\mathrm{Li}-\mathrm{O}(3)$ | $104 \cdot 8$ (3) |
| $\mathrm{O}(1)-\mathrm{Li}-\mathrm{O}\left(3^{\prime}\right)$ | 117.2 (3) |
| $\mathrm{O}(2)-\mathrm{Li}-\mathrm{O}(3)$ | $113 \cdot 1$ (3) |
| $\mathrm{O}(2)-\mathrm{Li}-\mathrm{O}\left(3^{\prime}\right)$ | $103 \cdot 5$ (3) |
| $\mathrm{O}(3)-\mathrm{Li}-\mathrm{O}\left(3^{\prime}\right)$ | 119.7 (2) |
| $\mathrm{NH}_{3} \mathrm{OH}$ ion |  |
| $\mathrm{N}-\mathrm{O}(5)$ | 1.400 (4) Å |
| $\mathrm{N}-\mathrm{H}(1)$ | 1.06 (3) |
| $\mathrm{N}-\mathrm{H}(2)$ | $0 \cdot 98$ (4) |
| $\mathrm{N}-\mathrm{H}(3)$ | $0 \cdot 96$ (4) |
| $\mathrm{O}(5)-\mathrm{H}(4)$ | 1.08 (6) |
| $\mathrm{H}(1)-\mathrm{N}-\mathrm{H}(2)$ | 102 (3) ${ }^{\circ}$ |
| $\mathrm{H}(1)-\mathrm{N}-\mathrm{H}(3)$ | 115 (3) |
| $\mathrm{H}(1)-\mathrm{N}-\mathrm{O}(5)$ | 116 (2) |
| $\mathrm{H}(2)-\mathrm{N}-\mathrm{H}(3)$ | 116 (3) |
| $\mathrm{H}(2)-\mathrm{N}-\mathrm{O}(5)$ | 107 (2) |
| $\mathrm{H}(3)-\mathrm{N}-\mathrm{O}(5)$ | 101 (3) |
| $\mathrm{H}(4)-\mathrm{O}(5)-\mathrm{N}$ | 89 (3) |

Views of the structure projected along a and $\mathbf{c}$ are shown in Figs. 1 and 2. The sulphur and lithium atoms are at the centre of oxygen tetrahedra which share corners to form the $\mathrm{LiSO}_{4}$ sheets perpendicular to [100].

Two hydrogen atoms of the $-\mathrm{NH}_{3}$ group and the

[^0]Table 4. Hydrogen-bond lengths and angles of the $\mathrm{NH}_{3} \mathrm{OH}$ ion

|  | D-H. ${ }^{\text {A }}$ |  | $\underset{(\AA)}{\mathrm{D}-\mathrm{H}}$ | $\underset{(\AA)}{H \cdots A}$ | D-A $(\AA)$ | $\underset{\left({ }^{\circ}\right)}{\mathrm{D}-\mathrm{H} \cdot \mathrm{~A}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| N | H(1) | $\mathrm{O}(2)$ |  | $\{1.75$ (3) | 2.799 (3) | 170 (3) |
| N | H(1) | $\mathrm{O}(4)$ |  | $\{2.38$ (4) | 3.066 (4) | 121 (2) |
| N | H(2) | $\mathrm{O}(4)$ | 0.98 (4) | 1.97 (4) | $2 \cdot 856$ (3) | 149 (3) |
| N | H(3) | $\mathrm{O}(4)$ | 0.96 (4) | 1.93 (4) | $2 \cdot 820$ (3) | 155 (4) |
| O(5) | H(4) | $\mathrm{O}(1)$ | 1.08 (6) | $1 \cdot 62$ (6) | $2 \cdot 656$ (3) | 158 (6) |

Table 5. Bond strengths in $\mathrm{LiNH}_{3} \mathrm{OHSO}_{4}$ : bond strengths in valence units and bond lengths in $\AA$ (in parentheses) for bonds between O and $\mathrm{Li}, \mathrm{S}$ and H
Bond strengths $(s)$ are calculated from the expression $s=\left(R / R_{0}\right)^{-N}$ where $R$ is the bond length:

|  |  | $\begin{aligned} & R_{0} \\ & N \end{aligned}$ | $\begin{aligned} & \mathrm{H}-\mathrm{O} \\ & 0.86^{*} \\ & 2 \cdot 17^{*} \end{aligned}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Li | S |  | H(1) | H(3) | H(3) | H(4) | Sums around anion |
| O(1) | $\begin{aligned} & 0.23 \\ & (1.975) \end{aligned}$ | $\begin{aligned} & 1.49 \\ & (1.478) \end{aligned}$ |  |  |  |  | $\underset{(1 \cdot 62)}{0 \cdot 25^{*}}$ | 1.97 |
| $\mathrm{O}(2)$ | $\begin{gathered} 0.25 \\ (1.939) \end{gathered}$ | $\begin{gathered} 1.50 \\ (1.476) \end{gathered}$ |  | $\stackrel{0.21^{*}}{(1.75)}$ |  |  |  | 1.96 |
| O(3) | $\begin{array}{cc} 0.24 & 0.23 \\ (1.957) & (1.981) \end{array}$ | $\begin{gathered} 1.48 \\ (1.480) \end{gathered}$ |  |  |  |  |  | 1.95 |
| O(4) |  | $\begin{gathered} 1.51 \\ (1.473) \end{gathered}$ |  | $\underset{(2 \cdot 38)}{0 \cdot 11^{*}}$ | $\underset{(1 \cdot 97)}{0 \cdot 17^{*}}$ | $\begin{gathered} 0 \cdot 17 * \\ (1 \cdot 93) \end{gathered}$ |  | 1.96 |
| Sums around cations | 0.95 | (198) |  |  |  |  |  |  |

* The parameters for H apply to bonds determined by neutron diffraction and will tend to underestimate the bond strength in this case.
hydrogen atom of the -OH group form hydrogen bonds with oxygen atoms of the nearest sheet. The remaining hydrogen atom of the $-\mathrm{NH}_{3}$ group, $\mathrm{H}(3)$, forms a hydrogen bond to $\mathrm{O}(4)$ of the opposite sheet. Details of the hydrogen bonds are given in Table 4.

The correctness of this structure is confirmed by the bond strength calculation (Brown \& Shannon, 1973) given in Table 5. Each oxygen atom of the sheet forms one strong bond ( 1.5 valence units) with a sulphur atom. The equivalence of the $\mathrm{Li}-\mathrm{O}$ and $\mathrm{H} \cdots \mathrm{O}$ bonds in terms of their strengths is seen in the way $O(1)$ and $\mathrm{O}(2)$ complete a threefold coordination by forming one bond to each Li and H while $\mathrm{O}(3)$ forms two bonds to Li and $\mathrm{O}(4)$ accepts three rather weak hydrogen bonds. The r.m.s. deviation of the sums of the bond strengths from the valence is 0.04 valence units.

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[^0]:    * A list of observed and calculated structure factors is given by Anderson (1973), and has also been deposited with the National Lending Library, England, as Supplementary Publication No. SUP 30162 ( 9 pp.). Copies may be obtained through the Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH 1 1NZ, England.

